

BESICOVITCH ALMOST AUTOMORPHIC SOLUTIONS OF NONAUTONOMOUS DIFFERENTIAL EQUATIONS OF FIRST ORDER

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ABSTRACT. The main purpose of this paper is to analyze the existence and uniqueness of Besicovitch almost automorphic solutions and weighted Besicovitch pseudo-almost automorphic solutions of nonautonomous differential equations of first order. We provide an interesting application of our abstract theoretical results.

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