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EXTENSION OF THE TRUNCATED BI-INDEXED WEIGHTED SHIFTS, RECURSIVENESS AND SUBNORMALITY

RAJAE BEN TAHER[1,*] and MUSTAPHA RACHIDI[2]

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Abstract. We build a process in order to extend the truncated weighted shift, using techniques of the bi-indexed recursive sequences. We apply this process to solve the subnormality of 2-variable weighted shifts, whose associated moment sequence is a bi-indexed recursive sequence. Notably, we detail the case of the truncated 2-variable weighted shift $T \equiv (T_1, T_2)$ of order $(2, 2)$.

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*Corresponding author.
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[1]Equip of EDA - Département de Mathématiques et Informatique, Faculté des Sciences,Université Moulay Ismail, B.P. 4010, Beni M'hamed, Méknés - Morocco.
Email address: bentaher89@hotmail.fr

[2]Instituto de Matemática INMA, UFMS, Av. Costa e Silva, Cidade Universitaria, Campo Grande - MS - Brazil.
Email address: mu.rachidi@gmail.com, mu.rachidi@hotmail.fr